Algorithm Theoretical Baseline Document: Level 2A dry temperature profiles

Version 2.3

18 October 2021

ROM SAF Consortium
Danish Meteorological Institute (DMI)
European Centre for Medium-Range Weather Forecasts (ECMWF)
Institut d’Estudis Espacials de Catalunya (IEEC)
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**DOCUMENT CHANGE RECORD**

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ROM SAF

The Radio Occultation Meteorology Satellite Application Facility (ROM SAF) is a decentralised processing centre under EUMETSAT which is responsible for operational processing of radio occultation (RO) data from the Metop and Metop-SG satellites and radio occultation data from other missions. The ROM SAF delivers bending angle, refractivity, temperature, pressure, humidity, and other geophysical variables in near real-time for NWP users, as well as reprocessed Climate Data Records (CDRs) and Interim Climate Data Records (ICDRs) for users requiring a higher degree of homogeneity of the RO data sets. The CDRs and ICDRs are further processed into globally gridded monthly-mean data for use in climate monitoring and climate science applications.

The ROM SAF also maintains the Radio Occultation Processing Package (ROPP) which contains software modules that aid users wishing to process, quality-control and assimilate radio occultation data from any radio occultation mission into NWP and other models.

The ROM SAF Leading Entity is the Danish Meteorological Institute (DMI), with Cooperating Entities: i) European Centre for Medium-Range Weather Forecasts (ECMWF) in Reading, United Kingdom, ii) Institut D'Estudis Espacials de Catalunya (IEEC) in Barcelona, Spain, and iii) Met Office in Exeter, United Kingdom. To get access to our products or to read more about the ROM SAF please go to: http://www.romsaf.org

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1. **Introduction**

1.1 **Purpose**

This ATBD document describes the algorithms used to derive the dry temperature products produced by the Radio Occultation Meteorology (ROM) Satellite Application Facility (SAF). The complete list of products covered by this ATBD is provided in Table 1.1. Note that this table includes (or may include) both products in development and products with operational status. The status of all ROM SAF data products is available at the website: [http://www.romsaf.org](http://www.romsaf.org)

The product requirements baseline is the PRD [AD.3]. The ATBD software package is based on the ROPP [RD.1].

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1 Detailed information on the different input data types and their version numbers can be found in the validation reports at [www.romsaf.org/product_documents.php](http://www.romsaf.org/product_documents.php).
1.2 Applicable and reference documents

1.2.1 Applicable documents
The following list contains documents with a direct bearing on the contents of this document:


[AD.2] CDOP-3 Cooperation Agreement: Agreement between EUMETSAT and DMI on the Third Continuous Development and Operations Phase (CDOP-3) of the Radio Occultation Meteorology Satellite Applications Facility (ROM SAF), Ref. EUM/C/85/16/DOC/19, approved by the EUMETSAT Council and signed at its 86th meeting on 7 December 2016


1.2.2 Reference documents
The following documents provide supplementary or background information, and could be helpful in conjunction with this document:


[RD.8] Algorithm Theoretical Baseline Document: Level 1B bending angles, Ref. SAF/ROM/DMI/ALG/BA/001


[RD.14] Syndergaard S (2012) Assessment of the Structural Uncertainty of GRAS Products from Level 1B (bending angles) up to Level 2 (temperatures), Final Report, Danish Meteorological Institute, EUMETSAT Contract No. EUM/CO/10/4600000745/AvE.


1.3 Acronyms and abbreviations

ATBD  Algorithm Theoretical Baseline Document
BA    Bending Angle
BAROCLIM  Bending Angle Radio Occultation Climatology
BUFR  Binary Universal Format for data Representation
CDAAC  COSMIC Data Analysis and Archival Center
CDOP  Continuous Development and Operations Phase
CDR  Climate Data Record
CHAMP  Challenging Mini-satellite Payload
COSMIC  Constellation Observing System for Meteorology, Ionosphere, and Climate
DMI  Danish Meteorological Institute
ECMWF  European Centre for Medium-range Weather Forecasts
EGM96  Earth Gravitational Model
EPS  EUMETSAT Polar satellite System
EPS-SG  EPS Second Generation
EUMETSAT  European organisation for the exploitation of METeorological SATellites
GNSS  Global Navigation Satellite System
GO  Geometric Optics
GPS  Global Positioning System (US)
GRACE  Gravity Recovery and Climate Experiment
GRAS  GNSS Receiver for Atmospheric Sounding (Metop instrument)
ICDR  Interim Climate Data Record
IEEC  Institut d’Estudis Espacials de Catalunya (Spain)
LEO  Low Earth Orbit
Metop  Meteorological Operational Polar satellite (EPS/EUMETSAT)
MSIS  Mass Spectrometer and Incoherent Scatter
NCO  Numerically Controlled Oscillator
NetCDF  Network Common Data Form
NRT  Near Real-Time
NTC  Non Time Critical
NWP  Numerical Weather Prediction
PP  Pre-Processor
PRD  Product Requirements Document
QC  Quality Control
RO  Radio Occultation
ROM SAF  Radio Occultation Meteorology SAF (EUMETSAT), former GRAS SAF
ROPP  Radio Occultation Processing Package
SAF  Satellite Application Facility (EUMETSAT)
SNR  Signal-to-noise ratio
WO  Wave Optics
1.4 Definitions

RO data products from the Metop, Metop-SG and Sentinel-6 satellites and RO data from other missions are grouped in data levels (level 0, 1, 2, or 3) and product types (NRT, Offline, NTC, CDR, or ICDR). The data levels and product types are defined below\(^2\). The lists of variables should not be considered as the complete contents of a given data level, and not all data may be contained in a given data level.

Data levels:

- **Level 0**: Raw sounding, tracking and ancillary data, and other GNSS data before clock correction and reconstruction;
- **Level 1A**: Reconstructed full resolution excess phases, total phases, pseudo ranges, SNRs, orbit information, I, Q values, NCO (carrier) phases, navigation bits, and quality information;
- **Level 1B**: Bending angles and impact parameters, tangent point location, and quality information;
- **Level 2**: Refractivity, geopotential height, “dry” temperature profiles (Level 2A), pressure, temperature, specific humidity profiles (Level 2B), surface pressure, tropopause height, planetary boundary layer height (Level 2C), ECMWF model level coefficients (Level 2D), quality information;
- **Level 3**: Gridded or resampled data, that are processed from Level 1 or 2 data, and that are provided as, e.g., daily, monthly, or seasonal means on a spatiotemporal grid, including metadata, uncertainties and quality information.

Product types:

- **NRT product**: Data product delivered less than: (i) 3 hours after measurement (ROM SAF Level 2 for EPS); (ii) 150 min after measurement (ROM SAF Level 2 for EPS-SG Global Mission); (iii) 125 min after measurement (ROM SAF Level 2 for EPS-SG Regional Mission);
- **Offline and NTC products**: Data product delivered from about 5 days to up to 6 months after measurement, depending on the applicable requirements. The evolution of this type of product is driven by new scientific developments and subsequent product upgrades;
- **CDR**: Climate Data Record generated from a dedicated reprocessing activity using a fixed set of processing software\(^3\). The data record covers an extended time period of several years (with a fixed end point) and constitutes a homogeneous data record appropriate for climate usage;
- **ICDR**: An Interim Climate Data Record (ICDR) regularly extends in time a (Fundamental or Thematic) CDR using a system having optimum consistency with and lower latency than the system used to generate the CDR\(^4\).

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\(^2\)Note that the level definitions differ partly from the WMO definitions: [http://www.wmo.int/pages/prog/sat/dataandproducts_en.php](http://www.wmo.int/pages/prog/sat/dataandproducts_en.php)

\(^3\) (i) GCOS 2016 Implementation Plan; (ii) [http://climatemonitoring.info/home/terminology/](http://climatemonitoring.info/home/terminology/)

\(^4\) [http://climatemonitoring.info/home/terminology/](http://climatemonitoring.info/home/terminology/) (the ICDR definition was endorsed at the 9th session of the joint CEOS/CAMS Working Group Climate Meeting on 29 March 2018)
1.5 Overview of this document

Chapter 2 gives a short algorithm overview, and Chapter 3 describes the technical details. Practical considerations such as validation method and quality control is given in Chapter 4, whereas assumptions and limitations are discussed in Chapter 5. Differences for NRT, Offline, NTC, CDR, and ICDR products are described in Chapter 6.
2. Algorithm overview

RO data may potentially have benchmarking quality for climate analyses because of the all-weather capability of the technique and because there is no need for calibration (as opposed to many other remote sensing instruments). However, RO processing is generally complex, not the least because different RO missions have different problems (such as low SNR, poor L2 tracking, data gaps, spikes, etc). Thus, besides the processing steps that can be easily described by equations, it is necessary to also have algorithms that can cope with a number of problematic issues. The algorithms in the Radio Occultation Processing Package (ROPP) have been developed over many years to do just that.

ROPP contains a module designed to compute ionospheric corrected bending angle, refractivity, and dry temperature profiles either from excess phase or L1 and L2 channel bending angle data derived from radio occultation measurements. A flow chart illustrating the ROPP pre-processor module is given in Figure 2.1. The main aspects of the algorithm for the Level 2A dry temperature are described in the ROPP pre-processor user guide [RD.1].

The algorithm description in this ATBD complements the ROPP user guide by focusing on details not described in the user guide or elsewhere. References to equations and sections in the user guide are provided when appropriate. Many of the algorithms in the ROPP pre-processor module are also described in [RD.2]. References to original work on which algorithms are based are provided in the relevant sections.

In the descriptions in Section 3.2, the specific choices of parameters that affect the outcome of the processing are mentioned, such as filter widths, vertical grids, parameters determining specifics in the processing, interpolation methods, etc. The values mentioned are either hard-coded in the software or set in a configuration file in the ROM SAF processing. Although these choices have influence on the results, and contribute to the structural uncertainty of the products, they are not considered to have any negative impact on the products and they do not compromise the benchmarking quality of the data.
Figure 2.1: Flow chart illustrating calling tree of the ROPP pre-processor occ tool to compute ionospheric corrected bending angle, refractivity, and dry temperature profiles from input L1 and L2 channel amplitude and phase measurements [RD.1].
3. Algorithm description

3.1 Physics of the problem

3.1.1 Fundamental observables
The fundamental observables measured by an RO instrument are the phase, \( L_i \), and amplitude, \( A_i \), of the Doppler-shifted incoming signal. Index \( i \) denotes one of the two GNSS signals, L1 (at frequency \( f_1 \)) and L2 (at frequency \( f_2 \)). The signal frequencies can vary depending on the GNSS constellation. Each occultation measurement is a time-series of measured phases and amplitudes as well as precise position information for the transmitter (GNSS) satellite and the receiver (LEO) satellite.

3.1.2 Doppler-shift and derived quantities
The received signal is Doppler-shifted due to the motion of the transmitter and receiver satellites. With known satellite positions and velocities this Doppler-shift may be calculated to high precision for the vacuum case. When the ray bends in the atmosphere the angles between the ray path and the directions of motion are slightly different than in the vacuum case, both for the transmitting and the receiving satellite. This leads to a slightly different Doppler-shift. From observed signal phases, the observed Doppler-shift may be found and from this (with precise knowledge of the satellite positions and velocities) the bending of the ray path through the atmosphere may be derived. This leads to a profile of bending angles as a function of impact parameter. Via the Abel transform the profile of bending angles as a function of impact parameter is converted to a profile of atmospheric refractive index as a function of altitude. For convenience results are given in terms of the refractivity \( N \) instead of the refractive index \( n \), with refractivity defined by \( N = 10^6 \cdot (n-1) \).

3.1.3 Relation to dry temperature
The refractivity is related to pressure, temperature, and humidity [RD.3; RD.4]. Assuming dry air and hydrostatic equilibrium, a temperature profile can be derived using the equation of state. Thus, we define \( N = \kappa_1 \cdot P_{\text{dry}} / T_{\text{dry}} \), where \( P_{\text{dry}} \) is called the dry pressure (not to be confused with the partial pressure of dry air), \( T_{\text{dry}} \) is called the dry temperature, and \( \kappa_1 = 77.6 \text{ N-unit·K·hPa}^{-1} \).

3.2 Mathematical description of the algorithm
Given a profile of refractivity as a function of altitude above the geoid, the following subsections describe the steps taken to obtain the dry temperature as a function of altitude above the geoid.

3.2.1 Hydrostatic integration
The dry temperature (and corresponding dry pressure) is obtained by ignoring the water vapor contribution to refractivity [RD.5]. Using the equation of state for an ideal gas and assuming hydrostatic equilibrium, the equation to be solved can be written (Eq. 4.21 in [RD.1]):
\[
\frac{d \ln P_{\text{dry}}}{dz} = f(z, \ln P_{\text{dry}}(z)) = -\frac{g(z)N(z)}{R \kappa_i \exp(\ln P_{\text{dry}}(z))},
\]

where \(g(z)\) is the gravitational acceleration as a function of altitude, \(z\), and \(R\) is the dry air gas constant. The dry pressure at each level is obtained using a fourth order Runge-Kutta method starting from the top at 150 km. The dry temperature readily follows as \(T_{\text{dry}} = \kappa_1 \cdot P_{\text{dry}} / N\). The integration step of the Runge-Kutta method is \(\sim 15\) m. During integration, the refractivity is interpolated (using spline interpolation of \(\log(N)\)) to the high-resolution levels. After the integration, temperature and pressure are interpolated back to the original levels (~100 m spacing).

### 3.2.2 Upper boundary condition

For initialization of the hydrostatic integration, the pressure at 150 km is calculated from the refractivity gradient at this altitude, disregarding the temperature gradient (Eq. 4.21 in [RD.1]).

### 3.3 Error sources

As a general consideration, the radio occultation signal consists of an excess phase and an amplitude. High-quality data is data with high SNR both in terms of amplitude and in terms of excess phase.

Amplitude noise is dominated by instrument noise under quiet ionospheric conditions. However, in the presence of ionospheric disturbances, or tilted sporadic E-layers, it can be severely affected by scintillations [RD.16]. Under quiet conditions the SNR is generally high except in the middle to lower troposphere, where the denser atmosphere leads to loss of signal intensity. This is particularly true when the humidity is high, which typically occurs in the tropics [RD.17]. This results in degraded bending angle data quality in the lower to middle troposphere, particularly in the tropics.

Besides instrument noise, the measured excess phase is affected by residual ionospheric noise [RD.18]. The ionospheric contribution to the signal is not fully removed by the ionospheric correction due to short timescale ionospheric variation and other higher order effects not accounted for in the residual correction. Since the measured excess phase signal is a function of atmospheric density it falls off approximately exponentially with impact height and so the noise comes to dominate the signal at high altitudes in the upper stratosphere and above. In the lower troposphere the tracking of the L2 signal becomes difficult and for that reason only the L1 signal is useful. This limits the accuracy of derived products.

The highest data quality is therefore found at intermediate altitudes of the higher troposphere to lower stratosphere, where the signal is strong both in terms of amplitude and in terms of excess phase.

Above a certain altitude in the upper stratosphere to lower mesosphere (depending on the noise level) the retrieved dry temperature is based on a merge between observations and a climatology. The implementation of the global search and fitting procedure in the
statistical optimization (see [RD.6]), together with an assumed standard deviation of the background error of 50%, should ensure very little bias influence from the climatology.
4. Practical considerations

4.1 Validation method

As a whole, the algorithms are used to process a number of occultation observations, which are then compared to the corresponding profiles extracted from ECMWF analyses and forecasts (forward modelled to dry temperature as a function of altitude above the geoid). The dry temperature profiles based on input data from CDAAC are also compared to the corresponding dry temperature profiles produced by CDAAC.

As the dry temperature is derived from the refractivity, which in turn is derived from the bending angle, the validation of all parts of the processing chain from bending angle to dry temperature is relevant to ensure the quality of the dry temperature. Many parts of the algorithms described here together with those described in [RD.6] and [RD.8], have been validated over many years, as similar versions of the algorithms have been used to produce results for scientific publications and reports (see [RD.2], [RD.5], [RD.7], [RD.12], [RD.13], [RD.14], [RD.19], and [RD.20]).

Certain parts have been modified over the past few years in the version of ROPP at DMI. These parts include an improvement to the search and fitting strategy to find a suitable background for the statistical optimization and the development and inclusion of the BAROCLIM model (Section 3.2.1 in [RD.6]). These modifications were validated by comparisons to data produced by the unmodified code, comparisons against ECMWF analyses, and comparisons to corresponding profiles from CDAAC. The algorithms have also been validated by comparing ‘raw’ and optimized bending angles. The latter approach is an efficient way to evaluate to which extent a potential bias from the climatology affects the retrievals. The generation and the validation of BAROCLIM for its use in radio occultation retrievals (though with a different search and fitting strategy than the one used here) can be found in [RD.15].

4.2 Quality control and diagnostics

The following quality control parameters are used to ensure the quality of the dry temperature products:

L2 quality score:

Measures the quality of the L2 signal. This score is defined as the maximum of an L2 penalty function over the interval 25–50 km (see [RD.8]). The L2 quality score is constructed such that a low value means high quality data.

Scaling factors:

The fitting of the background profile to the data at high altitudes results in two scaling factors (see [RD.6]). Usually the scaling factors are close to unity, but in cases of erroneous data, they can be off by large factors, and are therefore used as an additional quality check.

---

5 Explicit numbers for the QC settings can be found in the validation reports at www.romsaf.org/product_documents.php
LC weighting function:
The LC weighting function determined individually for each profile in the statistical optimization (see [RD.6]) is required to be sufficiently large below a given altitude (e.g., at least 0.9 at all altitudes below 40 km). The value indicates the fractional weight given to the data (as opposed to the background profile), and the weight increases rapidly downwards.

The L2 quality score, the scaling factors, and the LC weighting function are generated at different places in the code when the relevant parameters to generate them are readily available. They are output together with the data.

Besides checking the above quality control parameters, the following sanity checks are made to the data themselves:

- The independent variable (impact height for bending angle; altitude for refractivity and dry temperature) is required to vary monotonously.
- The bending angle and the refractivity are required to have valid values above and below certain impact heights/altitudes (e.g., above 60 km and below 20 km).
- The refractivity is required to be positive at all altitudes (the generation of the dry temperature will fail if it is not).
- At very high altitudes (e.g., above 60 km), the optimized bending angle is required to be within a certain threshold of the background profile used for statistical optimization.
- The bending angle, the refractivity, and the dry temperature, are compared to the corresponding profiles extracted from an NWP model (forward modeled to refractivity, dry temperature, and bending angle).

The dry temperature is marked as non-nominal if any of the above checks results in parameters or data values outside defined thresholds. The dry temperature is also marked as non-nominal if the incoming bending angle was marked as non-nominal.

4.3 Outputs

The output of the processing to dry temperature is a ROPP NetCDF file containing the following profile variables:

- Altitude above the geoid
- Geopotential height
- Dry temperature

The same NetCDF file contains the output from the bending angle [RD.8] and refractivity [RD.6] processing. A more complete and technical description of the output to the NetCDF file can be found in [RD.9].
5. Assumptions and limitations

5.1 Assumptions

5.1.1 Spherical symmetry
Radio occultation data are generally processed under the assumption of spherical symmetry. However, in principle this is only an apparent assumption because it depends on the interpretation of the retrieved profiles. If profiles are interpreted as representing the vertical structure in the atmosphere at a given fixed location, then the spherical symmetry assumption gives rise to a real error because the atmosphere is only approximately spherically symmetrical. If, on the other hand, retrieved profiles are interpreted as being weighted averages of the 3-dimensional (3D) atmosphere (primarily in the 2-dimensional (2D) occultation plane), the spherical symmetry assumption does not in principle give rise to any errors. This is why it could be an advantage to assimilate occultation data with 2D or 3D observation operators. Although the assimilation of dry temperature would be possible (with a suitable observation operator), it is not used in any known operational forecasting systems, and thus for all practical use, the spherical symmetry assumption gives rise to errors in the dry temperature.

5.1.2 The assumption of no water vapor
The dry temperature is not the actual (thermodynamic) temperature, but for all practical purposes it is the same as the actual temperature at altitudes where water vapour gives a negligible contribution to the refractivity (in practice above ~10 km depending on latitude; a rule of thumb is that the water vapour is negligible where the temperature is less than 240 K or at altitudes above the tropopause). However, even in the lower troposphere, where water vapour is normally abundant, the dry temperature can be considered a useful variable on its own, just as we consider the better-known virtual temperature a variable on its own. Thus the assumption of no water vapour can be considered just a way to define dry temperature.

5.1.3 Equation of state for an ideal gas
In the retrieval of dry temperature from refractivity it is assumed that the atmosphere is an ideal gas, which makes refractivity proportional to density. This is a very good assumption for most practical applications. Careful studies on the general accuracy of the relation between refractivity, pressure, temperature and water vapour can be found in [RD.4], [RD.10], and [RD.11]. There is not a unique conclusion on the best or most accurate values for the coefficients, and the issue is complicated by the fact that the coefficients seem to vary with atmospheric conditions.

5.1.4 Hydrostatic equilibrium
The dry pressure, and thus dry temperature, is obtained using the assumption of hydrostatic equilibrium. This is a very good assumption for most practical applications.

5.2 Algorithm limitations
The following subsections discuss limitations in the algorithms described in the corresponding subsections with the same titles in Section 3.2.
5.2.1 Upper boundary condition

In very rare cases the retrieved refractivity at very high altitudes is slightly negative (presumably related to the dynamical error estimation and ionospheric scintillations; see [RD.6]), which prevents further processing to dry temperature.
6. Description of differences for NRT, Offline, NTC, CDR and ICDR products

This chapter describes the parts of the algorithm which are different for NRT, Offline, NTC, CDR and ICDR products.

6.1 NRT

The algorithms used in NRT are equivalent to the ones described in Chapter 3. However, the dry temperature product is based on the refractivity product, which is derived in a different way in NRT than in offline (see [RD.6]).

6.2 Offline and NTC

The algorithms used for the Offline and NTC products are the ones described in Chapter 3.

6.3 CDR

The algorithms used for the CDR products are the same as the algorithms used in offline, but dry temperature is based on refractivity, which for the CDR does not include residual ionospheric correction (see [RD.6]).

6.4 ICDR

The algorithms used for the ICDR products are the same as the algorithms used for the CDR products.
Appendices

A.1 Description of how to run the code

The code is run by the following command (for offline and reprocessing):

ropp_pp_occ_tool <input_file> --no-ranchk -o <output_file> -c <config_file>

The input file is a ROPP NetCDF file containing high-resolution Level 1A data. The output file is a ROPP NetCDF file containing high-resolution Level 1B and 2A data.

A.2 Configuration file

An example of a ROPP PP configuration file is given below. The values of parameters are not necessarily the final ones that will be set in the offline and reprocessing of dry temperature.

# $Id: $
#****c* Configuration Files/metop_pp.cf *
# NAME
# metop_pp.cf - METOP data configuration file for pre-processor
# implementations in ROPP
# SYNOPSIS
# <pp_program> ... -c metop_pp.cf ...
# DESCRIPTION
# This file reflects the configuration for the PP
# implementations within ROPP suitable for use with METOP data.
# NOTES
# AUTHOR
# Met Office, Exeter, UK.
# Any comments on this software should be given via the ROM SAF
# Helpdesk at http://www.romsaf.org
# COPYRIGHT
# (c) EUMETSAT. All rights reserved.
# For further details please refer to the file COPYRIGHT
# which you should have received as part of this distribution.
#****

# 0. Output options
#-------------------------------------------------------------
output_lev1a = .false.    # Flag to output (modified) level 1a data
output_lev1b = .true.     # Flag to output level 1b data
output_lev2a = .true.     # Flag to output level 2a data
output_diag  = .true.     # Flag to output additional diagnostics

# 1. Excess phase to bending angle processing
#-------------------------------------------------------------
# 1.1 Occultation processing method
GO - use GEOMETRIC OPTICS processing to derive bending angle as a function of impact parameter from excess phase as a function of time.

WO - use WAVE OPTICS (CT2 algorithm) processing to derive bending angle as a function of impact parameter from excess phase as a function of time.

occ_method = WO

# 1.2 Filtering method
# ---------------------

optest - use OPTIMAL ESTIMATION: solution of integral equation
slpoly - use SLIDING POLYNOMIAL

filter_method = slpoly

# 1.3 Smoothing bending angle profile
# -----------------------------------

fw_go_smooth = 3000.0  # Filter width for smoothed GO bending angles (m)
fw_go_full = 3000.0    # Filter width for full resolution GO bending angles (m)
fw_wo = 2000.0        # Filter width for wave optics bending angle above 7 km (m)
fw_low = -1000.0       # Filter width for wave optics bending angle below 7 km (m)

# 1.4 Maximum height for wave optics processing
# -----------------------------------------------

hmax_wo = 25000.0     # Maximum height for wave optics processing (m)

# 1.5 Data cut-off limits
# -----------------------

Acut     = 0.0        # Fractional cut-off limit for amplitude
Pcut     = -2000.0    # Cut-off limit for impact height
Bcut     = 0.1        # Cut-off limit for bending angle
Hcut     = -250000.0  # Cut-off limit for straight-line tangent altitude

# 1.6 CT2 options
# ----------------

CFF      = 3           # Complex field filter flag (CFF = 'Pa')
dsh      = 200.0       # Shadow border width (m)

# 1.7 Degraded L2 data flag
# -------------------------

opt_DL2  = .true.

# 1.8 Compute and output spectra flag
# -----------------------------------

opt_spectra = .false.

# 1.9 Paths to EGM96 geoid model coefficients and corrections file
# -----------------------------------------------------------------

egm96 = ../data/egm96.dat                 # EGM96 coefficients file
corr_egm96 = ../data/corrcoef.dat         # Correction coefficients file

# 1. Ionospheric correction processing
# ---------------------------------------

# 1.1 Ionospheric correction method
# GMSIS - use MSIS climatology bending angle (searching global MSIS profiles
for best fit profile to obs) in ionospheric correction,
statistical optimization and bending angle to refractivity inversion.

# MSIS - use MSIS climatology bending angle in ionospheric correction,
statistical optimization and bending angle to refractivity inversion.

# GBARO - use BAROCLIM bending angle (searching global BAROCLIM profiles
for best fit profile to obs) in ionospheric correction,
statistical optimization and bending angle to refractivity inversion.

# BARO - use BAROCLIM bending angle in ionospheric correction,
statistical optimization and bending angle to refractivity inversion.

# BG - use climatology from a specified input file containing
background temperature, pressure and humidity
(e.g. from an NWP analysis). The input filename can be specified
using the '-bfile' command line argument or setting 'bfile' (see 1.5).

# NONE - linear combination of L1 and L2 bending angles in ionospheric
 correction, no additional information above observed profile top
in the inverse Abel to compute refractivity.

method = GBARO                # Ionospheric correction method

# 1.2 Abel integral method
# ------------------------

# LIN - assume linear variation of bending angle and ln(n) between
observation levels. This algorithm is used in ROM SAF NRT processing

# EXP - assume exponential variation of bending angle and ln(n) between
observation levels. This algorithm is used in ropp_fm module.

abel = LIN

# 1.3 Statistical optimisation method
# -----------------------------------

# SO - statistical optimisation.
# LCSO - linear combination plus statistical optimisation.

so_method = so

# 1.4 Climatology model coefficients files
# --------------------------------

msisfile = ../data/MSIS_coeff.nc           # MSIS coefficients file for phase model
mfile    = ../data/BAROCLIM_coeff.nc       # Model coefficients file for stat. opt.

# 1.5 Background model temperature, humidity, pressure file
# ---------------------------------------------------------

bfile    = BG_file.nc       # Background meteorology profile file (method=BG)

# 2. Impact parameter grid
# ---------------------------------------------------------

dpi = 100.0   # Step of standard impact parameter grid (m)

# 3. Smoothing bending angle profile
# -----------------------------------

# A smoothed bending angle profile is derived compute the fit of observed bending
# angles to the model bending angle profile.

np_smooth = 3  # Polynomial degree for smoothing regression

fw_smooth = 1000.0      # Filter width for smoothing profile
# 4. Model bending angle profile fit to observations

# To avoid systematic deviations from the observed profile with climatology, 
# the model profile is scaled to the observed profile by a fitting method.

sf_method = regular # Search and fit method (convoluted or regular)
nparm_fit = 2       # Number of parameters for model fit regression
hmin_fit = 40000.0  # Lower limit for model fit regression
hmax_fit = 60000.0  # Upper limit for model fit regression
omega_fit = 0.3    # A priori standard deviation of regression factor

# 5. Ionospheric correction and statistical optimization

# The method described by Gorbunov (2002) is implemented to perform ionospheric 
# correction with statistical optimization.

f_width = 50.0     # Ionospheric correction filter width
delta_p = 100.0   # Step of homogeneous impact parameter grid
s_smooth = 50.0    # External ionospheric smoothing scale
z_ion = 50000.0   # Lower height limit of ionospheric signal
z_str = 35000.0   # Lower height limit of stratospheric signal
z_ltr = 12000.0   # Lower height limit of tropospheric signal
n_smooth = 11     # Number of points for smoothing (must be odd)
model_err = 0.5   # A priori model error std.dev. (dyn.est. if negative)
opt_XL2 = .false. # L2 extrapolation on optimized bending angles

# 6. Bending angle inversion to refractivity

# The Abel inversion is computed to retrieve refractivity from corrected 
# bending angles. The corrected bending angle profile is extended 
# using MSIS or BAROCLIM data above the observed profile top.

ztop_invert = 150000.0 # Height of atmosphere top for inversion
dzh_invert = 50.0     # Step of inversion grid above observation top
dzr_invert = 20000.0  # Interval for regression in inversion

# 7. Tangent point lat-lons

# Set tp_bending=.true. to update lat-lons accounting for bending
tp_bending = .true.