# Towards an unbiased stratospheric temperature analysis

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#### How we observe stratospheric temperature



Radiosondes and RO are used as anchoring observations in the atmosphere

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### How we model stratospheric temperature (IFS)



Purpose of this talk is to demonstrate a new application of RO

 $\rightarrow$  RO used to diagnose temperature model biases

→ RO used to correct automatically those model biases in 4D-Var

#### Temperature bias in the operational IFS model (1/2)



# Temperature bias in the operational IFS model (2/2)

#### Temperature first-guess departure with respect to RO (~70hPa, January 2017)



→ model error is large scale and presents specific features



#### The bias is due to

- discretization errors in the vertical advection (dynamical core)
- inadequate representation of gravity waves in the vertical direction

RO can be used to diagnose the spatial structure of the model error

# 4D-Var assimilation (1/3)



#### Strong-constraint

- First-guess trajectory
- Observations
- Compute a correction at initial time
- Analysis trajectory

The model is assumed to be perfect (strong-constraint)

$$\mathbf{x}_k = \mathcal{M}_{k,k-1}(\mathbf{x}_{k-1}) \quad \text{for} \quad k = 1, \dots, N$$

Cost function depends only on the state at the beginning of the assimilation window

$$\begin{split} J(\mathbf{x}_0) &= \frac{1}{2} \left( \mathbf{x}_0 - \mathbf{x}_0^b \right)^{\mathrm{T}} \mathbf{B}^{-1} \left( \mathbf{x}_0 - \mathbf{x}_0^b \right) \\ &+ \frac{1}{2} \sum_{k=0}^{N} \left( \mathcal{H}_k \mathcal{M}_{k,0}(\mathbf{x}_0) - \mathbf{y}_k \right)^{\mathrm{T}} \mathbf{R}_k^{-1} \left( \mathcal{H}_k \mathcal{M}_{k,0}(\mathbf{x}_0) - \mathbf{y}_k \right) \end{split}$$

4D-Var assumes **random zero-mean errors** for all sources of information, but the IFS model has biases

# 4D-Var assimilation (2/3)

Unknown forcing is introduced (additive, Gaussian, constant within the assimilation window, no cross-correlation with the background error).

$$\mathbf{x}_k = \mathcal{M}_{k,k-1}(\mathbf{x}_{k-1}) + \eta$$
 for  $k = 1, \dots, N$ .



#### Weak-constraint

- First-guess trajectory
- Observations
- Compute a correction at initial time
- Compute a model forcing η
- Analysis trajectory

Cost function depends on the initial state and the model forcing

$$J(\mathbf{x}_{0}, \boldsymbol{\eta}) = \frac{1}{2} \left( \mathbf{x}_{0} - \mathbf{x}_{0}^{b} \right)^{\mathrm{T}} \mathbf{B}^{-1} \left( \mathbf{x}_{0} - \mathbf{x}_{0}^{b} \right)$$
$$+ \frac{1}{2} \left( \boldsymbol{\eta} - \boldsymbol{\eta}^{b} \right)^{\mathrm{T}} \mathbf{Q}^{-1} \left( \boldsymbol{\eta} - \boldsymbol{\eta}^{b} \right)$$
$$+ \frac{1}{2} \sum_{k=0}^{N} \left( \mathcal{H}_{k}(\mathbf{x}_{k}) - \mathbf{y}_{k} \right)^{\mathrm{T}} \mathbf{R}_{k}^{-1} \left( \mathcal{H}_{k}(\mathbf{x}_{k}) - \mathbf{y}_{k} \right)$$

#### 4D-Var assimilation (3/3)

$$egin{aligned} J(\mathbf{x}_0,oldsymbol{\eta}) &= rac{1}{2} \left( \mathbf{x}_0 - \mathbf{x}_0^b 
ight)^{\mathrm{T}} \mathbf{B}^{-1} \left( \mathbf{x}_0 - \mathbf{x}_0^b 
ight) \ &+ rac{1}{2} \left( oldsymbol{\eta} - oldsymbol{\eta}^b 
ight)^{\mathrm{T}} \mathbf{Q}^{-1} \left( oldsymbol{\eta} - oldsymbol{\eta}^b 
ight) \ &+ rac{1}{2} \sum_{k=0}^N \left( \mathcal{H}_k(\mathbf{x}_k) - \mathbf{y}_k 
ight)^{\mathrm{T}} \mathbf{R}_k^{-1} \left( \mathcal{H}_k(\mathbf{x}_k) - \mathbf{y}_k 
ight) \end{aligned}$$

 $\rightarrow$  method described in Sasaki (1970), never worked properly at a NWP centre

 $\rightarrow$  error statistics (B and Q) need to be specified



RO shows that model error (Q) is large scale

EDA shows that background error (B) is small scale

 $\rightarrow$  Scale separation

### Weak-constraint 4D-Var with scale separation in IFS (1/2)



→ temperature bias is reduced up to 50% (0.6C to 0.3C) with respect to radiosondes and GPS-RO

 $\rightarrow$  temperature RMSE is reduced by 6%

#### Weak-constraint 4D-Var with scale separation in IFS (1/2)



Cold biases in the lower/middle stratosphere over strong convective regions



Model error forcing from WC4DVAR at 70 hPa

→ correcting the bias from the missing gravity waves and the dynamical core

### Impact of new weak-constraint 4D-Var analysis on forecast skills





The better analysis can be seen in the forecasts

# Impact of new weak-constraint 4D-Var forcing on forecast skills





The model error estimation η is applied as a constant model forcing over 10 days
 The forecast model is not biased anymore and mean error does not increase
 Approach will be tested in seasonal forecast (some model error variability required)

### Conclusions and future work

#### New application of RO at ECMWF

- Diagnose model deficiencies and correct them in 4D-Var
- Bias reduced up to 50% with weak-constraint 4D-Var (from -0.6C to -0.3C)

How many RO do we need to estimate the model bias? Homogeneous network? What is the impact of weak-constraint 4D-Var on the observation bias correction? What is the best way to correct forecast/reanalysis bias? Climatology for η?